

$V_x = ?$

$$V_y - V_x = -V_1 \Rightarrow V_x = V_y + V_1$$

$$V_z + V_2 = V_x$$

$$V_z + V_2 = V_y + V_1$$

$$I_y + I_z + I_x = I$$

↓

$$V_x = A V_1 + B V_2 + C I$$

↑                      ↑                      ↑  
properties of the circuit

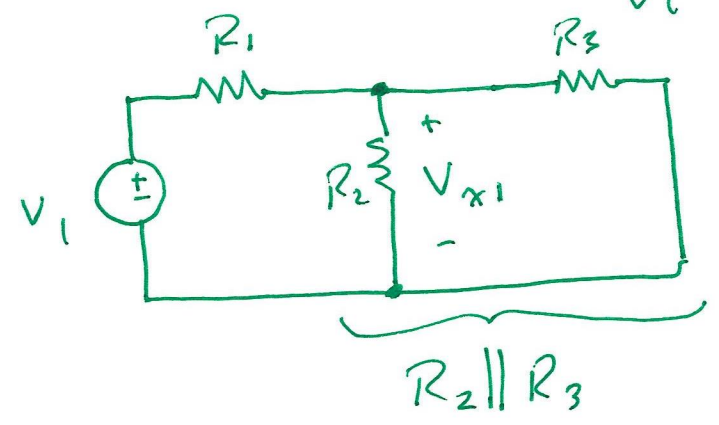
$$V_x = A V_1 + B V_2 + C I$$

Turn off  $V_2$  and  $I$

i.e.,  $V_2 = 0, I = 0$

Then  $V_{x1} = A V_1$

and  $A = \frac{V_x}{V_1}$

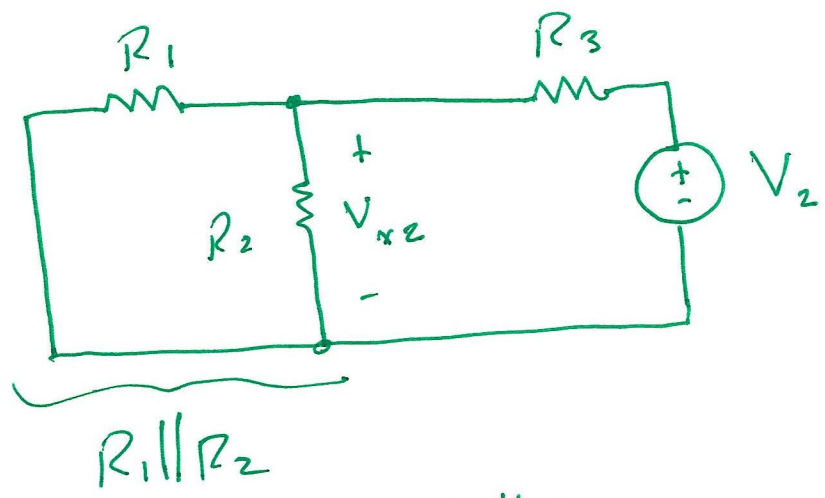


$$V_{x1} = \frac{R_2 \parallel R_3}{R_1 + (R_2 \parallel R_3)} V_1$$

A

To determine B:

Turn off  $V_1$  and  $\epsilon$ .

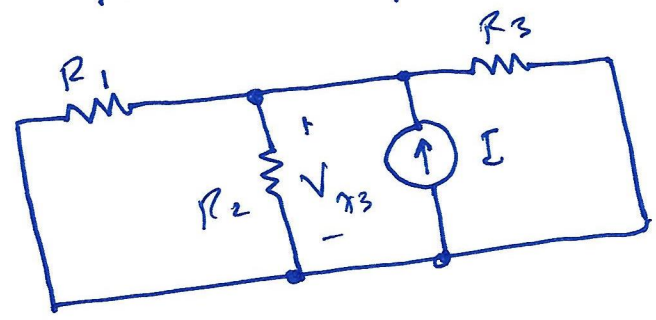


$$V_{xz} = \frac{R_1 || R_2}{R_3 + (R_1 || R_2)} \cdot V_2$$

B

To determine C:

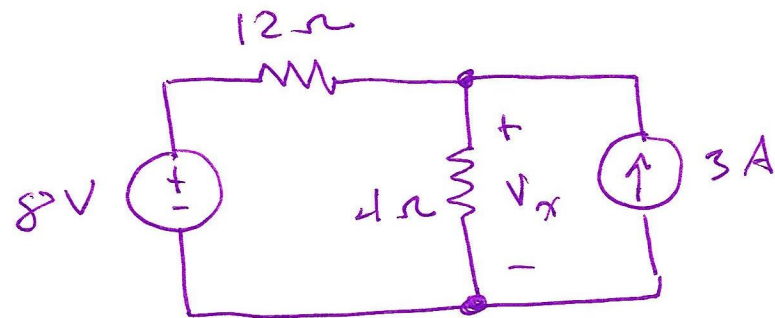
Turn off  $V_1$  and  $V_2$ .



$$V_{x3} = \underbrace{(R_1 \parallel R_2 \parallel R_3)}_C I$$

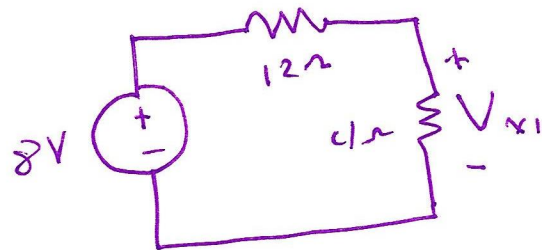
Then  $V_x = V_{x1} + V_{x2} + V_{x3}$

$$= \underbrace{\frac{R_2 \parallel R_3}{R_1 + (R_2 \parallel R_3)}}_A \cdot V_1 + \underbrace{\frac{R_3 \parallel R_2}{R_3 + (R_1 \parallel R_2)}}_B V_2 + \underbrace{(R_1 \parallel R_2 \parallel R_3)}_C \cdot I$$



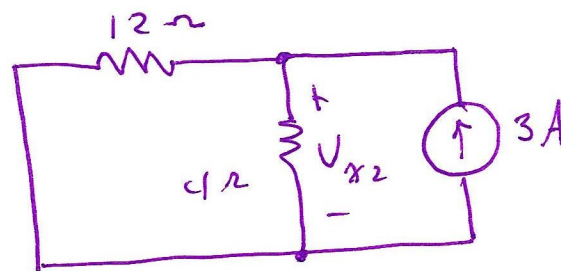
Using the superposition method,

① Solve for  $V_{x1}$



$$V_{x1} = \frac{4}{12+4} \cdot 8V = 2V$$

② Solve for  $V_{x2}$ :

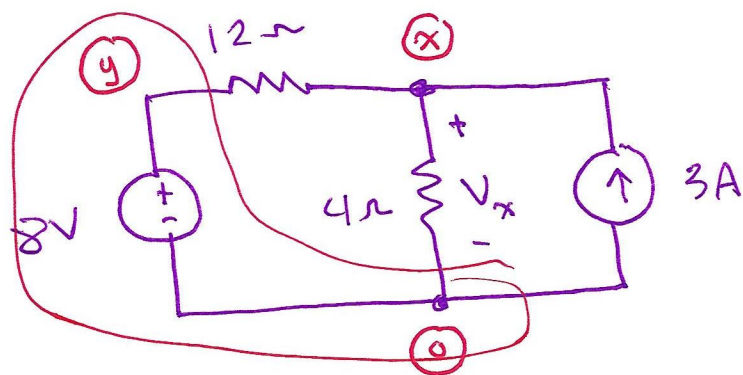


equivalent of  $12\Omega \parallel 4\Omega$

$$V_{x2} = (3\Omega)(3A) = 9V$$

③

$$V_x = V_{x1} + V_{x2} = 2V + 9V = 11V$$



Alternate solution:

Nodal Analysis

$$V_y = 8V$$

(constraint)

$$\frac{V_x - V_y}{12\Omega} + \frac{V_x}{4\Omega} - 3A = 0 \quad (\text{KCL at node } x)$$

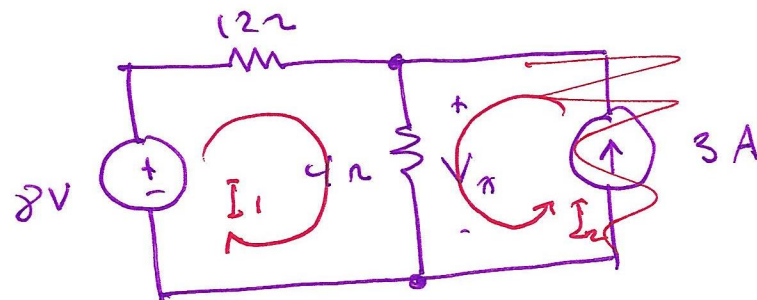
$$\frac{V_x - 8}{12} + \frac{V_x}{4} - 3 = 0$$

$$V_x - 8 + 3V_x - 36 = 0$$

$$4V_x = 44$$

$$V_x = 11V$$

## Mesh Analysis:



$$V_x = 4\Omega(I_1 + I_2)$$

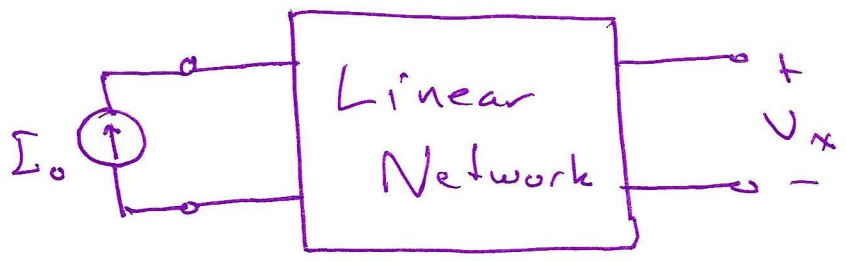
$$I_2 = 3A \quad (\text{constraint})$$

$$-8V + 12\Omega I_1 + 4\Omega(I_1 + I_2) = 0 \quad (\text{KVL})$$

$$16I_1 + 4 = 0$$

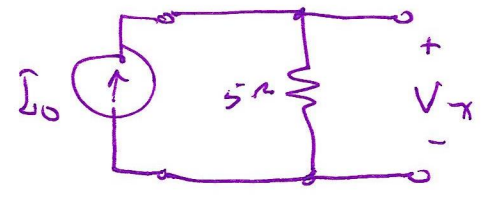
$$I_1 = -\frac{1}{4}A$$

$$V_x = 4\left(-\frac{1}{4} + 3\right) = \frac{11}{4} \cdot 4 = 11V$$



A linear network is made up of any combination of  $R$ ,  $VCCS$ ,  $VCVS$ ,  $CCVS$ ,  $CCCS$ .

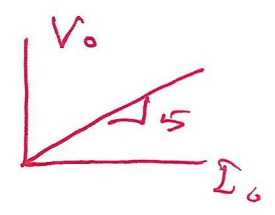
When the input is  $I_0$ , the output is  $V_x = 5I_0$ .



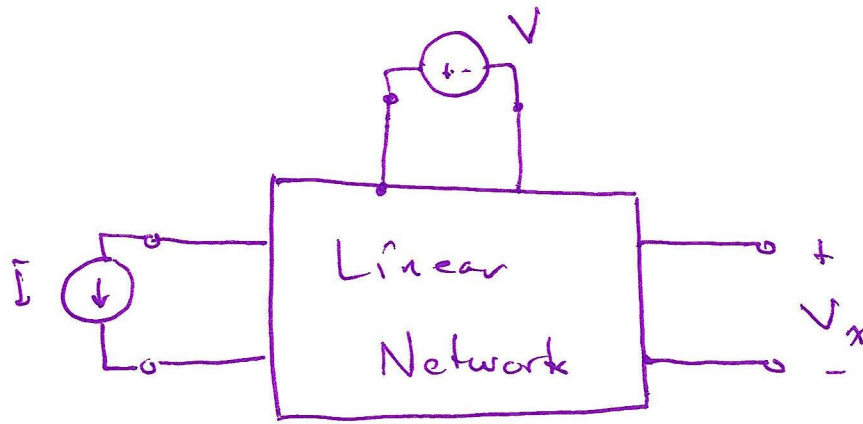
$$V_x = 5I_0$$

What is the output when  $I_0 = 2A$ ?      10V

What is the output when  $I_0 = 3A$ ?      15V







If  $V = 3V$  and  $I = 2A$ ,  $V_x = 7V$

If  $V = 4V$  and  $I = 3A$ ,  $V_x = 10V$

What will  $V_x$  be when  $V = 2V$  and  $I = 5A$ ?

$$V_x = A V + B I$$

$$7 = A 3 + B 2$$

$$10 = A 4 + B 3$$

$$3A + 2B = 7$$

$$4A + 3B = 10$$

$$\begin{bmatrix} 3 & 2 \\ 4 & 3 \end{bmatrix} \begin{bmatrix} A \\ B \end{bmatrix} = \begin{bmatrix} 7 \\ 10 \end{bmatrix}$$

Using Cramer's Rule:

$$A = \frac{\begin{vmatrix} 7 & 2 \\ 10 & 3 \end{vmatrix}}{\begin{vmatrix} 3 & 2 \\ 4 & 3 \end{vmatrix}} = \frac{21 - 20}{9 - 8} = \frac{1}{1} = 1$$

$$B = \frac{\begin{vmatrix} 3 & 7 \\ 4 & 10 \end{vmatrix}}{\begin{vmatrix} 3 & 2 \\ 4 & 3 \end{vmatrix}} = \frac{30 - 28}{1} = 2$$

$$V_x = 1 \cdot V + 2 \cdot I$$

So, when  $V = 2V$  and  $I = 5A$ ,

$$\begin{aligned} V_x &= 1(2V) + 2(5A) \\ &= 2 + 10 \\ &= 12V \end{aligned}$$